

Derivatives of the Trigonometric Functions

$$D_x [\sin x] = \cos x$$

$$D_x [\cos x] = -\sin x$$

$$D_x [\tan x] = \sec^2 x$$

$$D_x [\cot x] = -\operatorname{csc}^2 x$$

$$D_x [\sec x] = \sec x \tan x$$

$$D_x [\operatorname{csc} x] = -\operatorname{csc} x \cot x$$

$$f(x) = 3 \sin x$$

$$f'(x) = 3 \cos x$$

$$\frac{5x^3}{3 \cdot 5x^2}$$

$$h(x) = \tan x + \cot x$$

$$h'(x) = \sec^2 x - \csc^2 x$$

$$(\cos x) 3x^2$$

$$3x^2 \cos x$$

$$g(x) = x^3 \cos x$$

$$g'(x) = -\underline{x^3} \underline{\sin x} + \underline{3x^2} \underline{\cos x}$$

$$g'(x) = (x^3)(-\sin x) + (\cos x)(3x^2)$$

$$f(x) = 5 \sec x \tan x$$

$$\begin{aligned} f'(x) &= 5 \left[\sec x \sec^2 x + \tan x \sec x \tan x \right] \\ &= 5 \left[\sec^3 x + \sec x \tan^2 x \right] \end{aligned}$$

$$h(x) = \frac{2 \cos x}{1+x^2}$$

$$h'(x) = \frac{(1+x^2)(-2 \sin x) - (2 \cos x)(2x)}{(1+x^2)^2}$$