

Inverse Trigonometric Functions

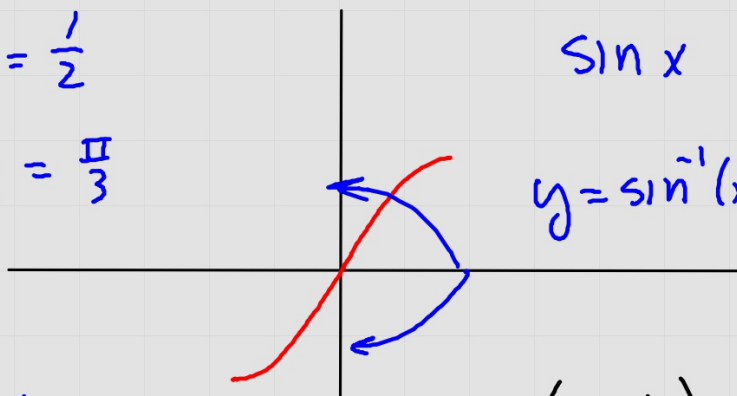
A Quick Review

$$\sin \frac{\pi}{3} = \frac{1}{2}$$

$$\sin^{-1} \frac{1}{2} = \frac{\pi}{3}$$

$$\sin x \quad D: \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$$

$$y = \sin^{-1}(x) \quad y \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$$



$$\sin^{-1} \left(-\frac{\sqrt{3}}{2} \right) = -\frac{\pi}{3}$$

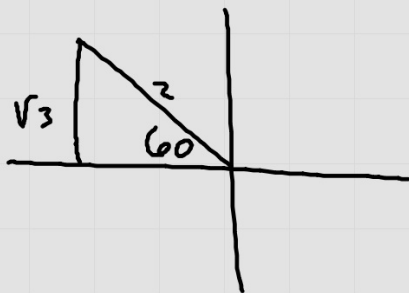
$$\sin(\sin^{-1} x) = x \quad x \in [-1, 1]$$

$$\sin^{-1}(\sin x) = x \quad x \in \left[-\frac{\pi}{2}, \frac{\pi}{2}\right]$$



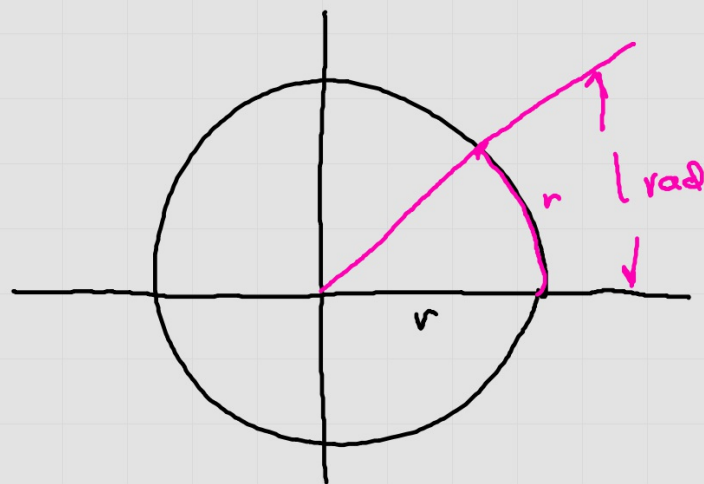
$$\sin^{-1}\left(\sin \frac{\pi}{3}\right) = \frac{\pi}{3}$$

$$\sin^{-1}\left(\sin \frac{2\pi}{3}\right) = \sin^{-1}\left(\frac{\sqrt{3}}{2}\right) = \frac{\pi}{3}.$$

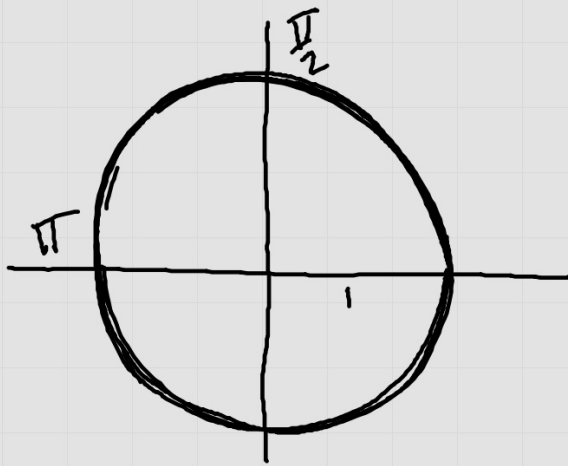


$$\arcsin(x) = \sin^{-1}(x)$$

$$\sin^{-1} \frac{1}{2}$$



$$C = 2\pi r$$



$$\cos x \quad D: [0, \pi]$$

$$y = \cos^{-1} x \quad y \in [0, \pi]$$

$$\cos(\cos^{-1} x) = x \quad x \in [-1, 1]$$

$$\cos^{-1}(\cos x) = x \quad x \in [0, \pi]$$

$$\cos^{-1}\left(\cos \frac{2\pi}{3}\right) = \frac{2\pi}{3}$$

$$\cos^{-1}\left(\cos \frac{11\pi}{12}\right) = \frac{11\pi}{12}$$

$$\cos^{-1}\left(\cos \frac{17\pi}{12}\right)$$

$$\tan(x) \quad D: \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$$

$$y = \tan^{-1}(x) \quad y \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$$

$$\tan(\tan^{-1}x) = x \quad x \in (-\infty, \infty)$$

$$\tan^{-1}(\tan x) = x \quad x \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$$

