

19. The figure above shows the graph of the function g and the line tangent to the graph of g at x = -1. Let h be the function given by  $h(x) = e^x \cdot g(x)$ . What is the value of h'(-1)?

(A) 
$$\frac{9}{e}$$
 (B)  $\frac{-3}{e}$  (C)  $\frac{-6}{e}$  (D)  $\frac{-6}{e} - \frac{3}{e^2}$  (E)  $-6$   
(A)  $\frac{9}{e}$  (B)  $\frac{-3}{e}$  (C)  $\frac{-6}{e}$  (D)  $\frac{-6}{e} - \frac{3}{e^2}$  (E)  $-6$   
(E)

$$\frac{1}{e} \left[ -6 + 3 \right]$$

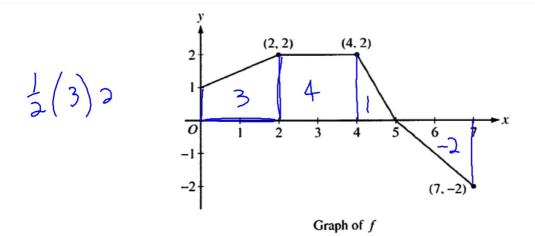
$$-\frac{3}{e}$$

20. For 
$$x > 0$$
,  $\frac{d}{dx} \left( \int_0^{2x} \ln(t^3 + 1) dt \right) =$ 

 $2 ln(8x^3+1) - ( )(0)$ 

- (A)  $\ln(x^3+1)$
- (B)  $\ln(8x^3 + 1)$
- (C)  $2\ln(x^3+1)$
- (D)  $2\ln(8x^3+1)$
- (E)  $24x^2 \ln(8x^3 + 1)$



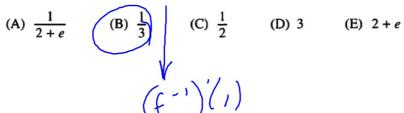


21. The graph of a function f is shown above. What is the value of  $\int_0^7 f(x) dx$ ?

- (A) 6
- (B) 8
- (C) 10
- (D) 14
- (E) 18

- 22. The function f is continuous for all real numbers, and the average rate of change of f on the closed interval [6, 9] is  $-\frac{3}{2}$ . For 6 < c < 9, there is no value of c such that  $f'(c) = -\frac{3}{2}$ . Of the following, which must be true?
  - (A)  $\frac{1}{3} \int_{6}^{9} f(x) dx = -\frac{3}{2}$
  - (B)  $\int_6^9 f(x) dx$  does not exist.
  - (C)  $\frac{f'(6) + f'(9)}{2} = -\frac{3}{2}$
  - (D) f'(x) < 0 for all x in the open interval (6, 9).
  - (E) f is not differentiable on the open interval (6, 9).

23. Let f be the function defined by  $f(x) = 2x + e^x$ . If  $g(x) = f^{-1}(x)$  for all x and the point (0,1) is on the graph of f, what is the value of g'(1)?



(f-1)(1)

Since (0,1) on  $f \to (f^{-1})'(i) = \frac{1}{f(0)}$   $f'(x) = 2 + e^{x}$ 

f'(0)=2+e°=3

24. The function g is given by  $g(x) = 4x^3 + 3x^2 - 6x + 1$ . What is the absolute minimum value of g on the closed interval [-2, 1]?

(A) 
$$-7$$
 (B)  $-\frac{3}{4}$  (C) 0 (D) 2  
 $9'/\chi = 12 \chi^{3} + 6 \chi - 6$ 

$$g(-2) = -32 + 12 + 12 + 1 = -7$$
  
 $g(1) = 4 + 3 - 6 + 1 =$ 

- 25. Which of the following is the solution to the differential equation  $\frac{dy}{dx} = e^{y+x}$  with the initial condition  $y(0) = -\ln 4$ ?
  - (A)  $y = -x \ln 4$
  - (B)  $y = x \ln 4$
  - (C)  $y = -\ln(-e^x + 5)$
  - (D)  $y = -\ln(e^x + 3)$
  - (E)  $y = \ln(e^x + 3)$

$$e^{-y}dy = e^{x}dx$$

$$-e^{-y} = e^{x} - S$$
  
 $e^{-y} = S - e^{x}$ 

$$e^{-y}dy = e^{x}dx$$
 $e^{-y} = e^{x} + c$ 
 $y = -\ln(5 - e^{x})$ 
 $y = -\ln(5 - e^{x})$ 

26. Which of the following is an antiderivative of 
$$f(x) = \sqrt{1+x^3}$$



(A) 
$$\frac{2}{3}(1+x^3)^{3/2}$$

(B) 
$$\frac{\frac{2}{3}(1+x^3)^{3/2}}{3x^2}$$

(C) 
$$\int_0^{1+x^3} \sqrt{t} \ dt$$

(D) 
$$\int_0^{x^3} \sqrt{1+t} \ dt$$

$$(E) \int_0^x \sqrt{1+t^3} \ dt$$

$$\frac{d}{dx} \int_{0}^{x} \sqrt{1+t^{3}} dt = \sqrt{1+x^{3}}$$

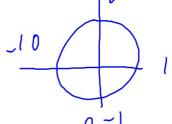
27. For time  $t \ge 0$ , the height h of an object suspended from a spring is given by  $h(t) = 16 + 7\cos\left(\frac{\pi t}{4}\right)$ . What is the average height of the object from t = 0 to t = 2?

(A) 16

(B) 
$$\frac{39}{2}$$

16 (B) 
$$\frac{39}{2}$$
 (C)  $16 - \frac{14}{\pi}$  (D)  $16 + \frac{14}{\pi}$ 

$$\frac{1}{2} \int_{0}^{2} \left[ \left( 16 + 7 \cos \frac{\pi}{4} + 1 \right) dt \right]$$



- 28. The function f is defined by  $f(x) = \sin x + \cos x$  for  $0 \le x \le 2\pi$ . What is the x-coordinate of the point of inflection where the graph of f changes from concave down to concave up?

- $\{ "(x) = \leq 1$  x wsx
- f"(x) = 0 -> SINX = (0) X
  - $X = \frac{3.17}{4} \alpha x = \frac{7.77}{4}$

 $\begin{cases} \frac{\pi}{4} & \text{(B)} \frac{3\pi}{4} & \text{(C)} \frac{5\pi}{4} & \text{(D)} \frac{7\pi}{4} & \text{(E)} \frac{9\pi}{4} & -\text{SMT-WST} \\ \begin{cases} \frac{7}{4} \\ \frac{1}{4} & \text{(D)} \\ \frac{7\pi}{4} & \text{(D)} \frac{7\pi}{4} & \text{(E)} \frac{9\pi}{4} & -\text{SMT-WST} \\ -\text{SIN} \frac{17}{2} - \omega S \frac{77}{2} & -\text{(D)} \\ -\text{(D)} & -\text{(D)} \\ -\text{(D)} & -\text{(D)} \\ -\text{(D)} & -\text{(D)} \\ -\text{(D)} & -\text{(D)} & -\text{(D)} \\ -\text{(D)} &$ 

