

19. The figure above shows the graph of the function g and the line tangent to the graph of g at x = -1. Let h be the function given by $h(x) = e^x \cdot g(x)$. What is the value of h'(-1)?

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$$h(x) = e^x \cdot g(x)$$
. What is the value of $h'(-1)$?

(A) $\frac{9}{e}$ (B) $\frac{-3}{e}$ (C) $\frac{-6}{e}$ (D) $\frac{-6}{e} - \frac{3}{e^2}$ (E) -6

$$h'(\chi) = e^{\chi} g'(\chi) + g(\chi) e^{\chi}$$

$$= e^{\chi} (g'(\chi) + g(\chi))$$

$$= e^{\chi} (g'(\chi) + g(\chi))$$

20. For
$$x > 0$$
, $\frac{d}{dx} \left(\int_0^{2x} \ln(t^3 + 1) dt \right) =$

(A)
$$\ln(x^3+1)$$

(B)
$$\ln(8x^3 + 1)$$

(B)
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(C) $2\ln(x^3 + 1)$

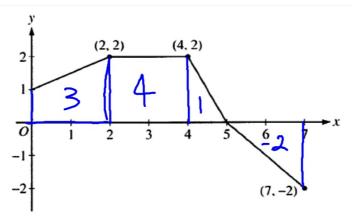
(D)
$$2\ln(8x^3+1)$$

(E)
$$24x^2 \ln(8x^3 + 1)$$

$$\frac{d}{dx} \int_{\gamma(x)}^{\eta(x)} f(t) dt = f(\eta(x)) h'(y) - f(g(x)) g'(x)$$

2 ln (8x3+1) - ()(0)





Graph of f

- 21. The graph of a function f is shown above. What is the value of $\int_0^7 f(x) dx$?
 - (A) 6
- (B) 8
- (C) 10
- (D) 14
- (E) 18

- 22. The function f is continuous for all real numbers, and the average rate of change of f on the closed interval [6, 9] is $-\frac{3}{2}$. For 6 < c < 9, there is no value of c such that $f'(c) = -\frac{3}{2}$ Of the following, which must be true?
 - (A) $\frac{1}{3} \int_{6}^{9} f(x) dx = -\frac{3}{2}$
 - (B) $\int_6^9 f(x) dx$ does not exist.
 - (C) $\frac{f'(6) + f'(9)}{2} = -\frac{3}{2}$
 - (D) f'(x) < 0 for all x in the open interval (6, 9).
 - (E) f is not differentiable on the open interval (6, 9),

23. Let f be the function defined by $f(x) = 2x + e^x$. If $g(x) = f^{-1}(x)$ for all x and the point (0,1) is on the graph of f, what is the value of g'(1)?

(B) $\frac{1}{3}$ (C) $\frac{1}{2}$ (D) 3 (E) 2 + e

(f-')'(1)

Sine (0,1) on f - (')'(1) = 1/(0)

f'(x)=2+e°=3

24. The function g is given by $g(x) = 4x^3 + 3x^2 - 6x + 1$. What is the absolute minimum value of g on the closed interval [-2, 1]?

(A) -7 (B) $-\frac{3}{4}$ (C) 0 (D) 2

 $2x^{2} + x - 1$

(2x-1)(x +1)

 $X = \frac{1}{2} nx = -1$

f(-2) = -32 +12+1=-7

f(1) = 4+3-6+1=

f(\frac{1}{2}) = \frac{1}{2} + \frac{2}{4} - 3 + 1 =

f(-1)=-4+3+6+1

25. Which of the following is the solution to the differential equation $\frac{dy}{dx} = e^{y+x}$ with the initial condition $y(0) = -\ln 4$?

$$(A) \quad y = -x - \ln 4$$

(B)
$$y = x - \ln 4$$

$$(C) y = -\ln(-e^x + 5)$$

$$(D) y = -\ln(e^x + 3)$$

(E)
$$y = \ln(e^x + 3)$$

$$\frac{dy}{dx} = e^{y}e^{x}$$

$$-e^{-3}=e^{\times}+c$$

$$-\frac{1}{e^{y}} = e^{x} - 5$$

$$\frac{1}{e^{y}} = 5 - e^{x}$$

$$-e^{-3} = e^{x} + c$$
 $e^{3} = (5-e^{x})^{-1}$

26. Which of the following is an antiderivative of $f(x) = \sqrt{1 + x^3}$?

(A)
$$\frac{2}{3}(1+x^3)^{3/2}$$

(B)
$$\frac{\frac{2}{3}(1+x^3)^{3/2}}{3x^2}$$

(C)
$$\int_0^{1+x^3} \sqrt{t} \ dt$$

$$(D) \int_0^{x^3} \sqrt{1+t} \ dt$$

$$(E) \int_0^x \sqrt{1+t^3} \ dt$$

$$\frac{\mathcal{Q}}{\mathcal{O}^{\chi}}\left(\int_{0}^{\chi}\sqrt{1+t^{3}}\,dx\right)$$

$$\sqrt{1+\chi^{3}}$$

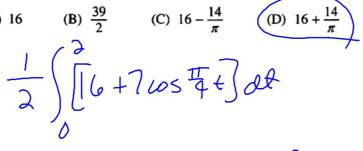
27. For time $t \ge 0$, the height h of an object suspended from a spring is given by $h(t) = 16 + 7\cos\left(\frac{\pi t}{4}\right)$. What is the average height of the object from t = 0 to t = 2?

(A) 16

(B)
$$\frac{39}{2}$$

(D)
$$16 + \frac{14}{\pi}$$

(E) $32 + \frac{28}{\pi}$



$$\frac{1}{2} \left[(32 + \frac{28}{11} \sin^{2} \frac{1}{2}) - (\frac{28}{11} \sin 0) \right]$$

$$\frac{1}{2} \left[(32 + \frac{28}{11} \sin^{2} \frac{1}{2}) - (\frac{28}{11} \sin 0) \right]$$

$$16 + \frac{14}{11}$$

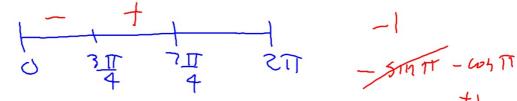
- 28. The function f is defined by $f(x) = \sin x + \cos x$ for $0 \le x \le 2\pi$. What is the x-coordinate of the point of inflection where the graph of f changes from concave down to concave up?

(A) $\frac{\pi}{4}$ (B) $\frac{3\pi}{4}$ (C) $\frac{5\pi}{4}$ (D) $\frac{7\pi}{4}$ (E) $\frac{9\pi}{4}$ $\left(\frac{7}{4}\right) = (0.5 \times - 5) \text{ Yr} \times$

 $f''(x) = -\sin x - \cos x$

 $(''/x) = 0 - \sin x = \cos x$

 $X = \frac{3\pi}{4} \alpha x = \frac{7\pi}{4}$



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