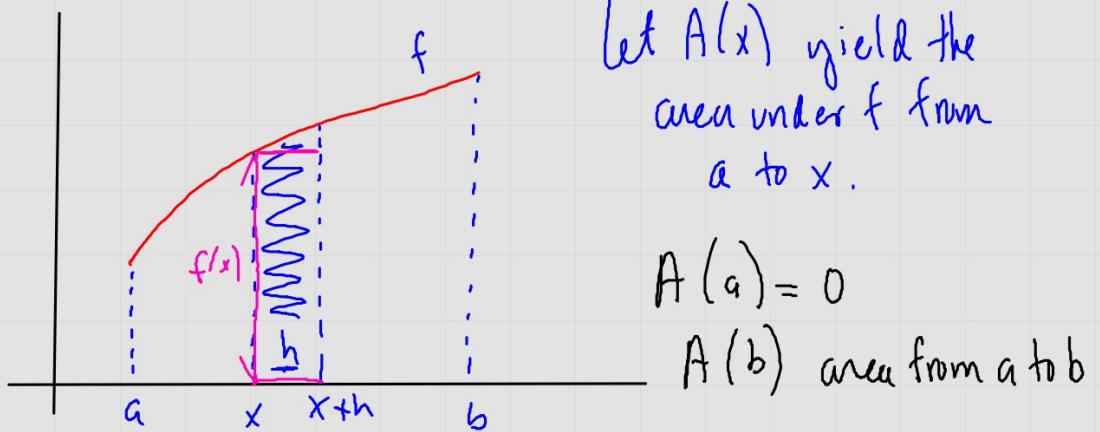


## The First Fundamental Theorem of Calculus



$$f(x) \cdot h \approx A(x+h) - A(x)$$

$$f(x) \approx \frac{A(x+h) - A(x)}{h}$$

$$\lim_{h \rightarrow 0} f(x) = \lim_{h \rightarrow 0} \frac{A(x+h) - A(x)}{h}$$

$$f(x) = A'(x)$$

$$\int f(x) dx = \underbrace{\int A'(x) dx}$$

$$A(x) = \int f(x) dx$$

Let  $F(x)$  be another anti. of  $f$  so,

$$A(x) = F(x) + C$$

$$A(a) = F(a) + C$$

$$C = -F(a)$$

$$A(x) = F(x) - F(a)$$

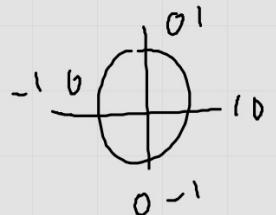
$$A(b) = \boxed{F(b) - F(a)}$$

1st Fun.  
Thm of  
Calc.

$$\int_a^b f(x) dx = F(b) - F(a) \quad \text{where } F'(x) = f(x)$$

$$\int_1^3 x^2 dx = \frac{1}{3} x^3 \Big|_1^3 = \frac{27}{3} - \frac{1}{3} = \frac{26}{3}.$$

$$\begin{aligned} \int_0^{2\pi} \sin x dx &= -\cos x \Big|_0^{2\pi} \\ &= (-\cos \pi) - (-\cos 0) \\ &= (-1) - (-1) \\ &= 0 \end{aligned}$$



$$\int_0^{\ln 3} e^x \sqrt{1+e^x} dx$$

~~$\frac{1}{3} \sqrt{1+e^x} \Big|_0^{\ln 3}$~~

$$\begin{aligned} u &= 1+e^x & x=0 & u=2 \\ du &= e^x dx & x=\ln 3 & u=4 \end{aligned}$$

$$\begin{aligned} \int_2^4 u^{1/2} du &= \frac{2}{3} u^{3/2} \Big|_2^4 \\ &= \frac{2\sqrt{u^3}}{3} \Big|_2^4 \\ &= \left( \frac{16}{3} \right) - \left( \frac{8}{3} \right) \\ &= \frac{16-8\sqrt{2}}{3} \end{aligned}$$

$$\int_{-1}^3 |x-2| dx$$

$$|x-2| = \begin{cases} x-2 & x \geq 2 \\ 2-x & x < 2 \end{cases}$$

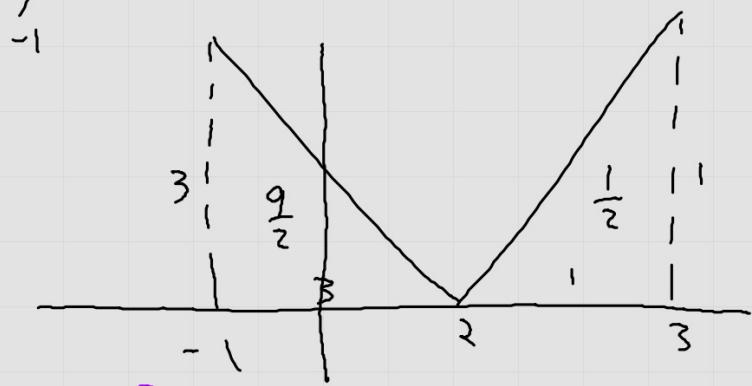
$$= \int_{-1}^2 (2-x) dx + \int_2^3 (x-2) dx$$

$$= \left[ 2x - \frac{1}{2}x^2 \right]_{-1}^2 + \left[ \frac{1}{2}x^2 - 2x \right]_2^3$$

$$= ( ) - ( ) + ( ) - ( )$$

DON'T

$$\int_{-1}^3 |x-2| dx$$



$$\int_{-1}^3 |x-2| dx = \frac{9}{2} + \frac{1}{2} = 5.$$

$$\begin{aligned}
 \int_1^3 (x^2 - x) dx &= \left[ \frac{1}{3}x^3 - \frac{1}{2}x^2 \right]_1^3 \\
 &= \left( \frac{27}{3} - \frac{9}{2} \right) - \left( \frac{1}{3} - \frac{1}{2} \right) \\
 &= \left( \cancel{\frac{27}{3}} \right) \left( -\cancel{\frac{9}{2}} \right) \left( -\cancel{\frac{1}{3}} \right) \left( +\cancel{\frac{1}{2}} \right) \\
 &= \frac{26}{3} - \frac{8}{2} \\
 &= \frac{26}{3} - \frac{12}{3} \\
 &= \frac{14}{3}.
 \end{aligned}$$