

On what interval(s) is $f(x) = x^3 - 9x^2 + 15x - 5$ increasing?

$$f'(x) = 3x^2 - 18x + 15$$

$$f' \geq 0 \quad \forall x$$

$$f'(x) = 0 \rightarrow x = 1 \text{ or } x = 5$$

f is increasing on $(-\infty, 1) \cup (5, \infty)$
because $f'(x) > 0$ on $(-\infty, 1) \cup (5, \infty)$.

Find the local ext. of $f(x) = x\sqrt{5-x^2}$

$$f'(x) = \frac{5-2x^2}{\sqrt{5-x^2}}$$

4
-4

$f' \neq 0$ on $(-\infty, -\sqrt{5}] \cup [\sqrt{5}, \infty)$

$$f'(x) = 0 \rightarrow x = -\frac{\sqrt{10}}{2} \text{ or } x = \frac{\sqrt{10}}{2}.$$

$$f''(x) = \frac{2x^3 - 15x}{\sqrt{(5-x^2)^3}}$$

f has a local min of $-\frac{5}{2}$ at $x = -\frac{\sqrt{10}}{2}$

because $f''(-\frac{\sqrt{10}}{2}) = 4 > 0 \rightarrow f$ is C.U.

f has a local max of $\frac{5}{2}$ at $x = \frac{\sqrt{10}}{2}$

because $f''(\frac{\sqrt{10}}{2}) = -4 < 0 \rightarrow f$ is C.D.

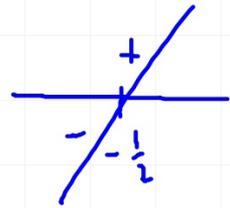
Find IPs (if any) of $f(x) = 2x^3 + 3x^2 - 12x + 1$

$$f'(x) = 6x^2 + 6x - 12$$

$$f''(x) = 12x + 6$$

$$f'' \neq 0 \forall x$$

$$f''(x) = 0 \text{ when } x = -\frac{1}{2}.$$



f has IP at $(-\frac{1}{2}, \frac{15}{2})$ because

$$f''(x) < 0 \text{ on } (-\infty, -\frac{1}{2}) \text{ and}$$

$$f''(x) > 0 \text{ on } (-\frac{1}{2}, \infty) \text{ and } f(-\frac{1}{2}) = \frac{15}{2}.$$

Use SDT to find relext. of $f(x) = -4x^3 + 3x^2 + 18x$

$$f'(x) = -12x^2 + 6x + 18$$

$$f' \exists \forall x$$

$$f'(x) = 0 \rightarrow x = -1 \text{ or } x = \frac{3}{2}$$

30
-30

$$f''(x) = -24x + 6$$

f has a relmin of -11 at $x = -1$ because
 $f''(-1) = 30 > 0 \rightarrow f$ is C.U.

f has a relmax of $\frac{81}{4}$ at $x = \frac{3}{2}$ because
 $f''(\frac{3}{2}) = -30 < 0 \rightarrow f$ is C.D.