

On what interval(s) is $f(x) = x^3 - 9x^2 + 15x - 5$ increasing?

$$f'(x) = 3x^2 - 18x + 15$$

$$f' \exists \forall x$$

$$f'(x) = 0 \Rightarrow x = 1 \text{ or } x = 5$$

f is incr. on $(-\infty, 1) \cup (5, \infty)$

because $f'(x) > 0$ on $(-\infty, 1) \cup (5, \infty)$.

⁴
-1 Find the local ext. of $f(x) = x\sqrt{5-x^2}$

$$f'(x) = \frac{5-2x^2}{\sqrt{5-x^2}}$$

$f' \neq 0$ on $(-\infty, -\sqrt{5}] \cup [\sqrt{5}, \infty)$

$$f'(x) = 0 \rightarrow x = -\frac{\sqrt{10}}{2} \text{ or } x = \frac{\sqrt{10}}{2}$$

$$f''(x) = \frac{2x^3 - 15x}{\sqrt{(5-x^2)^3}}$$

f has a rel min of $-\frac{5}{2}$ at $x = -\frac{\sqrt{10}}{2}$

because $f''(-\frac{\sqrt{10}}{2}) = 4 > 0 \rightarrow f$ is C.U.

f has a rel max of $\frac{5}{2}$ at $x = \frac{\sqrt{10}}{2}$

because $f''(\frac{\sqrt{10}}{2}) = -4 < 0 \rightarrow f$ is C.D.

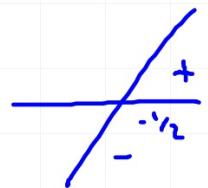
Find IP_s (if any) of $f(x) = 2x^3 + 3x^2 - 12x + 1$

$$f'(x) = 6x^2 + 6x - 12$$

$$f''(x) = 12x + 6$$

$$f'' \exists \forall x$$

$$f''(x) = 0 \Rightarrow x = -\frac{1}{2}$$



f has IP at $(-\frac{1}{2}, \frac{15}{2})$ because

$f''(x) < 0$ on $(-\infty, -\frac{1}{2})$ and

$f''(x) > 0$ on $(-\frac{1}{2}, \infty)$ and $f(-\frac{1}{2}) = \frac{15}{2}$.

Use SOT to find next. of $f(x) = -4x^3 + 3x^2 + 18x$

$\text{so } f'(x) = -12x^2 + 6x + 18$

$f' \exists \forall x$

$f'(x) = 0 \rightarrow x = -1 \text{ or } x = \frac{3}{2}$

$f''(x) = -24x + 6$

f has rel min of -11 at $x = -1$

because $f''(-1) = 30 > 0 \rightarrow f$ is C.U.

f has a rel max of $\frac{81}{4}$ at $x = \frac{3}{2}$

because $f''\left(\frac{3}{2}\right) = -30 < 0 \rightarrow f$ is C.D.