

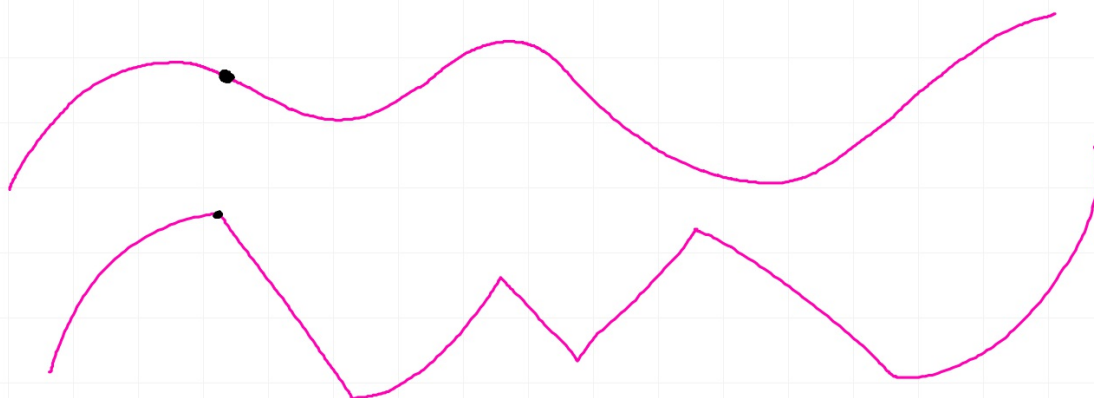
Continuity

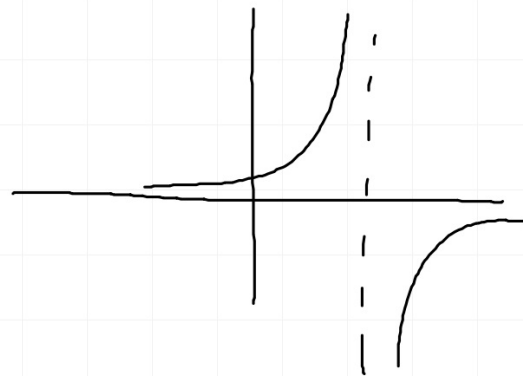
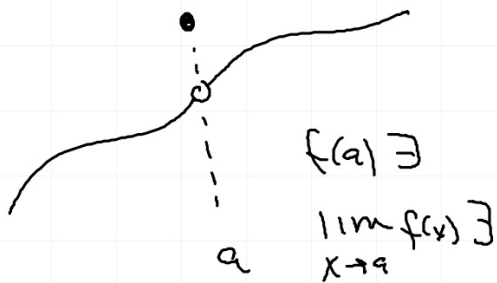
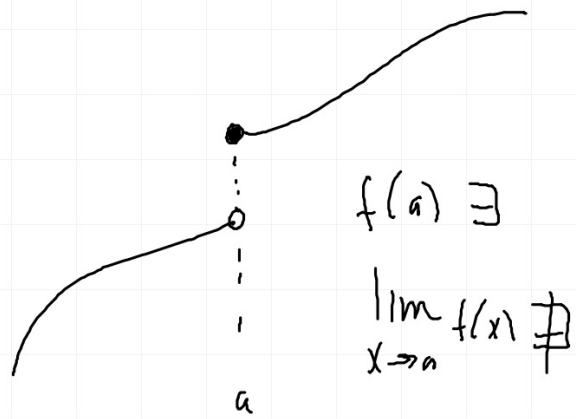
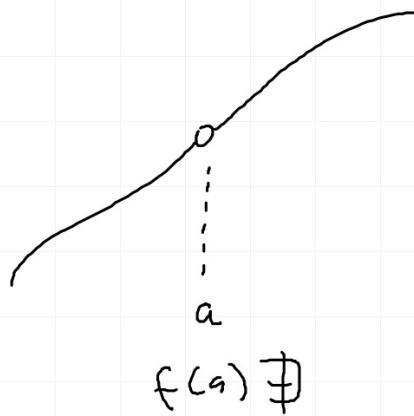


at a number



on an interval





f is cont. at $x=a$ iff

$$f(a) \exists$$

$$\lim_{x \rightarrow a} f(x) \exists$$

$$f(a) = \lim_{x \rightarrow a} f(x)$$

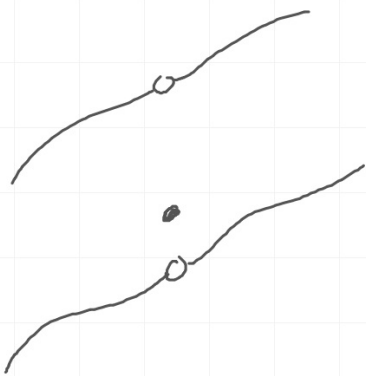
$$Is \ f(x) = \frac{x^2 + 2x - 15}{x - 3} \text{ cont. at } x = 3?$$

Cont test at $x = 3$

$$f(3) \nexists \therefore f \text{ is}$$

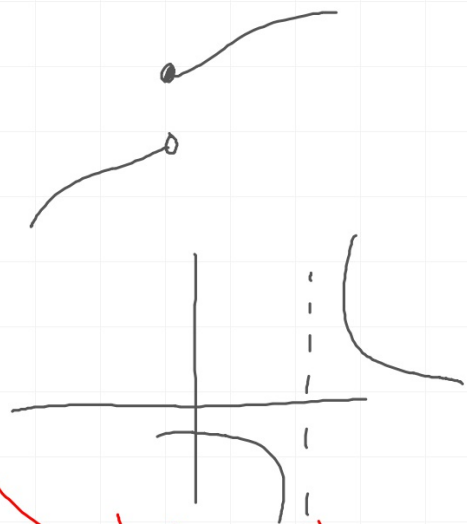
discon. at $x = 3$.

Removable disc



if $\lim_{x \rightarrow s} f(x) \exists$

Essential disc



if $\lim_{x \rightarrow s} f(x) \nexists$

$$15 \quad f(x) = \begin{cases} x^2 & x \leq 2 \\ 2x & x > 2 \end{cases} \quad \text{cont at } x=2?$$

Cont test at $x=2$

$$f(2) = 4$$

$$\left. \begin{array}{l} \lim_{x \rightarrow 2^+} f(x) = 4 \\ \lim_{x \rightarrow 2^-} f(x) = 4 \end{array} \right\} \therefore \lim_{x \rightarrow 2} f(x) = 4$$

$\therefore f$ is cont at $x=2$ because

$$f(2) = \lim_{x \rightarrow 2} f(x).$$

$$15 \quad f(x) = \begin{cases} x^2 - 9 & x \leq 7 \\ 5 + x & x > 7 \end{cases} \quad \text{cont at } x=7?$$

Cont test at $x=7$

$$f(7) = 40$$

$$\lim_{x \rightarrow 7^+} f(x) = 12$$

$$\lim_{x \rightarrow 7^-} f(x) = 40$$

$$\left. \begin{array}{l} \lim_{x \rightarrow 7^+} f(x) = 12 \\ \lim_{x \rightarrow 7^-} f(x) = 40 \end{array} \right\} \therefore \lim_{x \rightarrow 7} f(x) \nexists$$

$\therefore f$ is discon. at $x=7$ because $\lim_{x \rightarrow 7} f(x) \nexists$.

Determine if $f(x) = \begin{cases} x^2 - 49 & x \leq -7 \\ 49 - x^2 & -7 < x < 7 \\ 5 - x & x \geq 7 \end{cases}$ is cont $\forall x$.

Cont test at $x = -7$

$$f(-7) = 0$$

$$\left. \begin{array}{l} \lim_{x \rightarrow -7^+} f(x) = 0 \\ \lim_{x \rightarrow -7^-} f(x) = 0 \end{array} \right\} \therefore \lim_{x \rightarrow -7} f(x) = 0$$

$\therefore f$ is cont at $x = -7$

because $f(-7) = \lim_{x \rightarrow -7} f(x)$.

Cont test at $x = 7$

$$f(7) = -2$$

$$\left. \begin{array}{l} \lim_{x \rightarrow 7^+} f(x) = -2 \\ \lim_{x \rightarrow 7^-} f(x) = 0 \end{array} \right\} \therefore \lim_{x \rightarrow 7} f(x) \nexists$$

$\therefore f$ is discon at $x = 7$

because $\lim_{x \rightarrow 7} f(x) \nexists$.

For what value of b will $f(x) = \begin{cases} \frac{x^2 - 25}{x - 5} & x \neq 5 \\ b & x = 5 \end{cases}$
be cont at $x = 5$?

Cont test at $x = 5$

$$f(5) = b$$

$$\lim_{x \rightarrow 5} f(x) = 10$$

for f to be cont. at $x = 5 \rightarrow b = 10$.

Determine if $f(x) = \frac{x^2 + 2x - 15}{x - 3}$ is cont at $x = 3$. If
disc. determine if discon is removable or essential.
If removable, redefine f so that it is cont at $x = 3$.

Cont test at $x = 3$

$f(3) \nexists \therefore f$ is
discon. at $x = 3$.

Removable (Essen)

The discon is removable
because $\lim_{x \rightarrow 3} f(x) = 8$.

Redefine f

$$f(x) = \begin{cases} \frac{x^2 + 2x - 15}{x - 3} & x \neq 3 \\ 8 & x = 3 \end{cases}$$

$$f(x) = \frac{x-5}{x-3}$$

Is f cont on $[3, 5]$ no

$(3, 5)$ yes

$(-2, 3]$ no

$(1, 8)$ no