- 76. A particle moves along the x-axis so that at any time  $t \ge 0$  its velocity is given by  $v(t) = t^2 \ln(t+2)$ . What is the acceleration of the particle at time t = 6?
  - (A) 1.500
- (B) 20.453
- (C) 29.453
- (D) 74.860
- (E) 133.417

$$y = V(t)$$
  
 $y^2 = a(y((x), x))$   
 $y^2(6)$ 

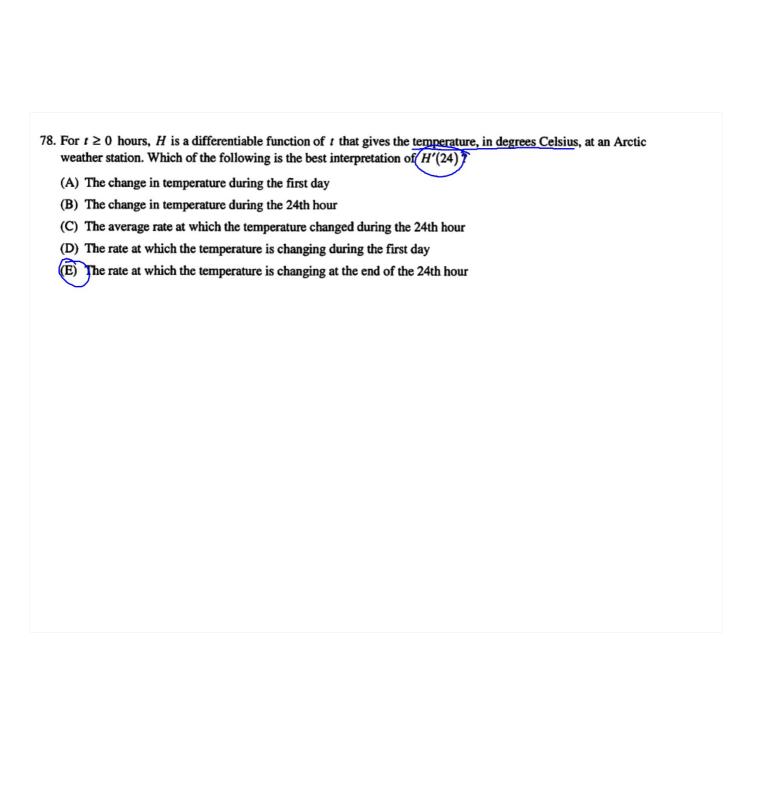
- 77. If  $\int_0^3 f(x) dx = 6$  and  $\int_3^5 f(x) dx = 4$ , then  $\int_0^5 (3 + 2f(x)) dx = 6$ (A) 10 (B) 20 (C) 23 (D) 35

- (E) 50

$$\int_{0}^{5} 3 dx + 2 \int_{0}^{5} f(x) dx$$

$$3(5-0) + 2(10)$$





79. A spherical tank contains 81.637 gallons of water at time t = 0 minutes. For the next 6 minutes, water flows out of the tank at the rate of  $9\sin(\sqrt{t+1})$  gallons per minute. How many gallons of water are in the tank at the end of the 6 minutes?

(A) 36.606

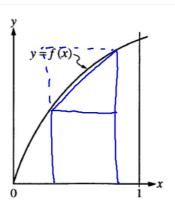
(B) 45.031

(C) 68.858

(D) 77.355

(E) 126.668

 $81.637 - \int_{0}^{6} 9 \sin \sqrt{t+1} dt = 36.606$ 



Rieman overlunder iner. or dear. Trap our lunde con up c dunn

- 80. A left Riemann sum, a right Riemann sum, and a trapezoidal sum are used to approximate the value of  $\int_0^1 f(x) dx$ , each using the same number of subintervals. The graph of the function f is shown in the figure above. Which of the sums give an underestimate of the value of  $\int_0^1 f(x) dx$ ?
  - I. Left sum 🗸
  - II. Right sum OVC
  - III. Trapezoidal sum 🗸
  - (A) I only
  - (B) II only
  - (C) III only
  - (D) I and III only
  - (E) II and III only

81. The first derivative of the function f is given by  $f'(x) = x - 4e^{-\sin(2x)}$ . How many points of inflection does the graph of f have on the interval  $0 < x < 2\pi$ ?

(A) Three

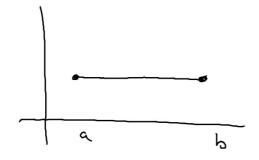
- (B) Four
- (C) Five
- (D) Six
- (E) Seven

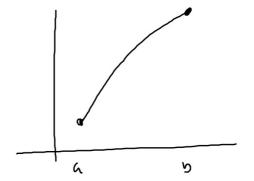
grouph f' on 0 to 277 count # rel. ext.

- 82. If f is a continuous function on the closed interval [a, b], which of the following must be true?
  - There is a number c in the open interval (a, b) such that f(c) = 0.
  - There is a number c in the open interval (a, b) such that f(a) < f(c) < f(b).
  - There is a number c in the closed interval [a, b] such that  $\underbrace{f(c) \ge f(x)}$  for all x in [a, b].

    (D) There is a number c in the open interval (a, b) such that  $\underbrace{f'(c) \ge 0}$ .

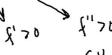
    - (E) There is a number c in the open interval (a, b) such that  $\underline{f'(c)} = \frac{f(b) f(a)}{b a}$ .





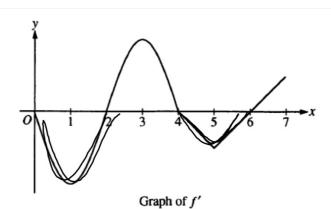
x	2.5	2.8	3.0	3.1	
f(x)	31.25	39.20	45	48.05	

- 83. The function f is differentiable and has values as shown in the table above. Both f and f' are strictly increasing on the interval  $0 \le x \le 5$ . Which of the following could be the value of f'(3)?
  - (A) 20
- (B) 27.5
- (C) 29
- (E) 30.5

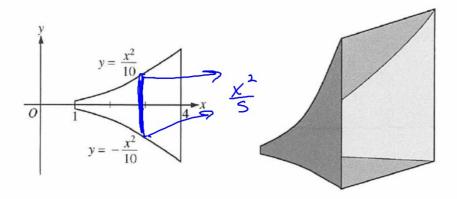


$$\frac{45 - 39.2}{3 - 2.8} = 29$$

$$\frac{48.05 - 45}{3.1 - 3} = 30.5$$



84. The graph of f', the derivative of the function f, is shown above. On which of the following intervals is f decreasing?



- 85. The base of a loudspeaker is determined by the two curves  $y = \frac{x^2}{10}$  and  $y = -\frac{x^2}{10}$  for  $1 \le x \le 4$ , as shown in the figure above. For this loudspeaker, the cross sections perpendicular to the x-axis are squares. What is the volume of the loudspeaker, in cubic units?

- (E) 25.711

The rights above. For this foldspeaker, the cross sections perpendicular volume of the loudspeaker, in cubic units?

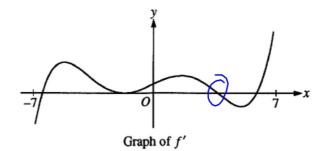
(B) 
$$4.092$$
 (C)  $4.200$  (D)  $8.184$ 

(C)  $4.200$  (D)  $4.184$ 

x	3	4	5	6	7			
f(x)	20	17	12	16 _	_ 20			
	C.	, ,	-1,	11-	C( > 0			

86. The function f is continuous and differentiable on the closed interval [3, 7]. The table above gives selected values of f on this interval. Which of the following statements must be true?

- I. The minimum value of f on [3, 7] is 12.
- II. There exists c, for 3 < c < 7, such that f'(c) = 0.
- III. f'(x) > 0 for 5 < x < 7.
- (A) I only
- (B) II only
- (C) III only
- (D) I and III only
- (E) I, II, and III



87. The figure above shows the graph of f', the derivative of the function f, on the open interval -7 < x < 7. If f' has four zeros on -7 < x < 7, how many relative maxima does f have on -7 < x < 7?

- (A) One
- (B) Two
- (C) Three
- (D) Four
- (E) Five

- 88. The rate at which water is sprayed on a field of vegetables is given by  $R(t) = 2\sqrt{1 + 5t^3}$ , where t is in minutes and R(t) is in gallons per minute. During the time interval  $0 \le t \le 4$ , what is the average rate of water flow, in gallons per minute?
  - (A) 8.458
- (B) 13.395

- (E) 35.833

(C) 14.691 (D) 18.916 (E) 35.1

$$\frac{1}{4-0}$$
 | P(1) at = 14.691

х	f(x)	f'(x)	g(x)	g'(x)
1	3	-2	-3	4

89. The table above gives values of the differentiable functions f and g and their derivatives at x = 1. If

The table above gives values of the differentiable function 
$$h(x) = (2f(x) + 3)(1 + g(x))$$
, then  $h'(1) =$ 
(A) -28 (B) -16 (C) 40 (D) 44

$$h'(x) = [2+(x)+3][g'(x)] + [1+g(x)][2+(x)]$$
  
 $h'(x) = [2+(x)+3][g'(x)] + [1+g(x)][2+(x)]$  = 44

90. The functions f and g are differentiable. For all x, f(g(x)) = x and g(f(x)) = x. If f(3) = 8 and f'(3) = 9, what are the values of g(8) and g'(8)?

(A) 
$$g(8) = \frac{1}{3}$$
 and  $g'(8) = -\frac{1}{9}$ 

(B) 
$$g(8) = \frac{1}{3}$$
 and  $g'(8) = \frac{1}{9}$ 

(C) 
$$g(8) = 3$$
 and  $g'(8) = -9$ 

(D) 
$$g(8) = 3$$
 and  $g'(8) = -\frac{1}{9}$   
(E)  $g(8) = 3$  and  $g'(8) = \frac{1}{9}$ 

(E) 
$$g(8) = 3$$
 and  $g'(8) = \frac{1}{9}$ 

$$\mathfrak{J}'(8) = \frac{1}{5}$$

$$= \frac{1}{9}$$

- 91. A particle moves along the x-axis so that its velocity at any time  $t \ge 0$  is given by  $v(t) = 5te^{-t} 1$ . At t = 0, the particle is at position x = 1. What is the total distance traveled by the particle from t = 0 to t = 4?
  - (A) 0.366
- (B) 0.542

- (E) 2.821

ition x = 1. What is the total distance of the property of

- 92. Let f be the function with first derivative defined by  $f'(x) = \sin(x^3)$  for  $0 \le x \le 2$ . At what value of x does f attain its maximum value on the closed interval  $0 \le x \le 2$ ?
  - (A) 0

(B) 1.162 (C) 1.465 (D) 1.845 (E) 2

graph f' above to he low.