

1. Since $v(t) = 3 - 2t \rightarrow s(t) = 3t - t^2 + C$.

We know $s(0) = 4 \rightarrow C = 4$.

$\therefore s(t) = 3t - t^2 + 4$.

2. Since $v(t) = 3t^{1/2} \rightarrow s(t) = 2t^{3/2} + C$.

We know $s(1) = 5 \rightarrow C = 3$.

$\therefore s(t) = 2t^{3/2} + 3$.

3. Since $a(t) = \cos t + \sin t \rightarrow v(t) = \sin t - \cos t + C$.

We know $v(0) = 5 \rightarrow C = 6$.

$\therefore v(t) = 6 + \sin t - \cos t$.

Since $v(t) = 6 + \sin t - \cos t \rightarrow s(t) = 6t - \cos t - \sin t + D$.

We know $s(0) = 0 \rightarrow D = 1$.

$\therefore s(t) = 6t + 1 - \cos t - \sin t$.

4. Velocity Function

$a(t) = -9.8 \rightarrow v(t) = -9.8t + C$

Since $v(0) = 0 \rightarrow C = 0$.

$\therefore v(t) = -9.8t$.

Position Function

Since $v(t) = -9.8t \rightarrow s(t) = -4.9t^2 + D$.

We know $s(0) = 450 \rightarrow D = 450$.

$\therefore s(t) = -4.9t^2 + 450$.

Time to Impact

At impact $s(t) = 0 \rightarrow 0 = -4.9t^2 + 450 \rightarrow t \approx -9.583$ or $t \approx 9.583$.

We choose $t \approx 9.583$ $\therefore$ it takes approximately 9.583 seconds to hit the ground.

Velocity at Impact

$v(9.583) \approx -93.915$ $\therefore$ the velocity at impact is approximately -93.915 meters per second.

5. Velocity Function

$$a(t) = -32 \longrightarrow v(t) = -32t + C$$

$$\text{Since } v(0) = -64 \longrightarrow C = -64.$$

$$\therefore v(t) = -32t - 64.$$

Position Function

$$\text{Since } v(t) = -32t - 64 \longrightarrow s(t) = -16t^2 - 64t + D.$$

$$\text{We know } s(0) = 80 \longrightarrow D = 80.$$

$$\therefore s(t) = -16t^2 - 64t + 80.$$

Time to Impact

$$\text{At impact } s(t) = 0 \longrightarrow 0 = -16t^2 - 64t + 80 \longrightarrow t = -5 \text{ or } t = 1.$$

We choose $t = 1$ $\therefore$ it takes one second to hit the ground.

Velocity at Impact

$$v(1) = -96 \therefore \text{ the velocity at impact is approximately -96 feet per second.}$$

6. Velocity Function

$$a(t) = -32 \longrightarrow v(t) = -32t + C$$

$$\text{Since } v(0) = 40 \longrightarrow C = 40.$$

$$\therefore v(t) = -32t + 40.$$

Position Function

$$\text{Since } v(t) = -32t + 40 \longrightarrow s(t) = -16t^2 + 40t + D.$$

$$\text{We know } s(0) = 60 \longrightarrow D = 60.$$

$$\therefore s(t) = -16t^2 + 40t + 60.$$

Time to Maximum Height

$$\text{At maximum height } v(t) = 0 \longrightarrow 0 = -32t + 40 \longrightarrow t = 1.250.$$

$\therefore$ it takes 1.250 seconds to reach the maximum height.

Maximum Height

$$s(1.250) = 85 \therefore \text{ the maximum height is 85 feet.}$$

Time to Impact

$$\text{At impact } s(t) = 0 \longrightarrow 0 = -16t^2 + 40t + 60 \longrightarrow t \approx -1.055 \text{ or } t \approx 3.555.$$

We choose 3.555 $\longrightarrow$ it takes approximately 3.555 seconds to hit the ground.

Velocity at Impact

$$v(3.555) \approx -73.756 \therefore \text{ the velocity at impact is approximately -73.756 feet per second.}$$

7. Velocity Function Ball #1

Since $a(t) = -32 \rightarrow v(t) = -32t + C$.

We know $v(0) = 48 \rightarrow C = 48 \rightarrow v(t) = -32t + 48$.

Position Function Ball #1

Since $v(t) = -32t + 48 \rightarrow s(t) = -16t^2 + 48t + D$.

We know $s(0) = 423 \rightarrow D = 423 \rightarrow s(t) = -16t^2 + 48t + 423$.

Velocity Function Ball #2

Since $a(t) = -32 \rightarrow v(t) = -32t + C$.

We know $v(1) = 24 \rightarrow C = 56 \rightarrow v(t) = -32t + 56$.

Position Function Ball #1

Since $v(t) = -32t + 56 \rightarrow s(t) = -16t^2 + 56t + D$.

We know $s(1) = 423 \rightarrow D = 383 \rightarrow s(t) = -16t^2 + 56t + 383$

Time to Pass

Because we want the positions to be the same we set the position functions equal to each other.

$$-16t^2 + 48t + 423 = -16t^2 + 56t + 383 \rightarrow t = 5.$$

$\therefore$ the balls pass each other 5 seconds after the first ball is thrown. At this time they are 263 feet off the ground.