

1. $f(1) = 1$

$$f'(x) = 3x^2 \longrightarrow f'(1) = 3$$

$$L(x) = 1 + 3(x - 1)$$

2. $f(0) = \frac{1}{\sqrt{2}}$

$$f'(x) = -\frac{1}{2\sqrt{(2+x)^3}} \longrightarrow f'(0) = -\frac{1}{4\sqrt{2}}$$

$$L(x) = \frac{1}{\sqrt{2}} - \frac{1}{4\sqrt{2}}(x - 0)$$

3. $f(4) = \frac{1}{4}$

$$f'(x) = -\frac{1}{x^2} \longrightarrow f'(4) = -\frac{1}{16}$$

$$L(x) = \frac{1}{4} - \frac{1}{16}(x - 4)$$

4. $f(-8) = -2$

$$f'(x) = \frac{1}{3\sqrt[3]{x^2}} \longrightarrow f'(-8) = \frac{1}{12}$$

$$L(x) = -2 + \frac{1}{12}(x + 8)$$

5. $f(0) = 1$

$$f'(x) = \frac{1}{2\sqrt{1+x}} \longrightarrow f'(0) = \frac{1}{2}$$

$$L(x) = 1 + \frac{1}{2}(x - 0)$$

6. $f(0) = 0$

$$f'(x) = \cos x \longrightarrow f'(0) = 1$$

$$L(x) = x$$

7. $f(0) = 1$

$$f'(x) = -\frac{8}{(1+2x)^5} \longrightarrow f'(0) = -8$$

$$L(x) = 1 - 8x$$

8. $f(0) = 1$

$$f'(x) = -\frac{1}{2\sqrt{1-x}} \longrightarrow f'(0) = -\frac{1}{2}$$

$$L(x) = 1 - \frac{1}{2}x$$

To find $\sqrt{0.9}$ we need to evaluate the linearization at an x such that $1 - x = .9 \longrightarrow x = .1$

$$L(.1) = .950 \quad \therefore \sqrt{0.9} \approx .950$$

To find $\sqrt{0.99}$ we need to evaluate the linearization at an x such that $1 - x = .99 \longrightarrow x = .01$

$$L(.01) = .995 \quad \therefore \sqrt{0.99} \approx .995$$

9. $g(0) = 1$

$$g'(x) = \frac{1}{3\sqrt[3]{(1+x)^2}} \longrightarrow g'(0) = \frac{1}{3}$$

$$L(x) = 1 + \frac{1}{3}x$$

To find $\sqrt[3]{0.95}$ we need to evaluate the linearization at an x such that $1 + x = .95 \longrightarrow x = -.05$

$$L(-.05) = .983 \quad \therefore \sqrt[3]{0.95} \approx .983$$

To find $\sqrt[3]{1.1}$ we need to evaluate the linearization at an x such that $1 + x = 1.1 \longrightarrow x = .1$

$$L(.1) = 1.033 \quad \therefore \sqrt[3]{1.1} \approx 1.033$$