

AP CALCULUS
THE LIMIT OF A FUNCTION

1. (a) $\lim_{x \rightarrow 4^+} f(x) = 3$
(b) $\lim_{x \rightarrow 4^-} f(x) = 3$
(c) $\lim_{x \rightarrow 4} f(x) = 3$
(d) $\lim_{x \rightarrow -1^+} f(x) = 2$
(e) $\lim_{x \rightarrow -1^-} f(x) = -2$
(f) $\lim_{x \rightarrow -1} f(x) \nexists$
(g) $f(-1) = 2$
(h) $f(a)$ is not always the same as $\lim_{x \rightarrow a} f(x)$

2. (a) $\lim_{x \rightarrow 4^+} f(x) = 6$
(b) $\lim_{x \rightarrow 4^-} f(x) = 2$
(c) $\lim_{x \rightarrow 4} f(x) \nexists$
(d) $f(4) = 4$
(e) $\lim_{x \rightarrow -5^+} f(x) = 0$
(f) $\lim_{x \rightarrow -5^-} f(x) \nexists$
(g) $\lim_{x \rightarrow -5} f(x) \nexists$
(h) $f(-5) = 0$

3. (a) $\lim_{x \rightarrow 0^-} f(x) = 1$
(b) $\lim_{x \rightarrow 0^+} f(x) = 1$
(c) $\lim_{x \rightarrow 0} f(x) = 1$
(d) $f(0) = 1$

4. $\lim_{x \rightarrow 1} g(x) = \frac{1}{3}$

5. $\lim_{x \rightarrow 0} f(x) = \frac{1}{2}$

6. $\lim_{x \rightarrow 5^+} \frac{1}{x-5} = +\infty$ Same as \nexists only more specific.

7. $\lim_{x \rightarrow 3} \frac{1}{(x-3)^8} \nexists$ Note: $\lim_{x \rightarrow 3^+} \frac{1}{(x-3)^8} = +\infty$ and $\lim_{x \rightarrow 3^-} \frac{1}{(x-3)^8} = +\infty$